

**Unit 2A Exam Review - Quadratic Equations**

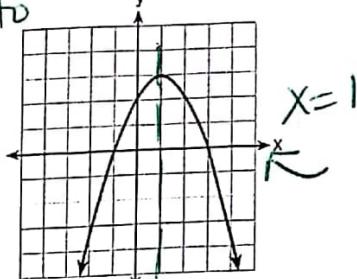
**Multiple Choice** - Identify the choice that best completes the statement or answers the question. Make sure to show ALL work to receive full credit.

1. Factored completely, the expression  $2x^2 + 10x - 12$  is equivalent to

- a.  $2(x - 6)(x + 1)$
- b.  $2(x + 6)(x - 1)$
- c.  $2(x + 2)(x + 3)$
- d.  $2(x - 2)(x - 3)$

$$2(x^2 + 5x - 6) \xrightarrow{\text{add to } 2} 2(x+6)(x-1)$$

4. Which parabola has an axis of symmetry of  $x = 1$ ?



2. Which relation is *not* a function?

- a.  $\{(2, 4), (1, 2), (0, 0), (-1, 2), (-2, 4)\}$
- b.  $\{(2, 4), (1, 1), (0, 0), (-1, 1), (-2, 4)\}$  (X cannot repeat to be a function)
- c.  $\{(2, 2), (1, 1), (0, 0), (-1, 1), (-2, 2)\}$
- d.  $\{(2, 2), (1, 1), (0, 0), (1, -1), (-2, -2)\}$

3. What is the vertex of the graph of the equation

$y = 3x^2 + 6x + 1$ ? \*Use calc or put

- a.  $(-1, -2)$
- b.  $(-1, 10)$
- c.  $(1, -2)$
- d.  $(1, 10)$

$$-1 = 3(x^2 + 2x + 1) \quad \left(\frac{2}{2}\right)^2$$

+3

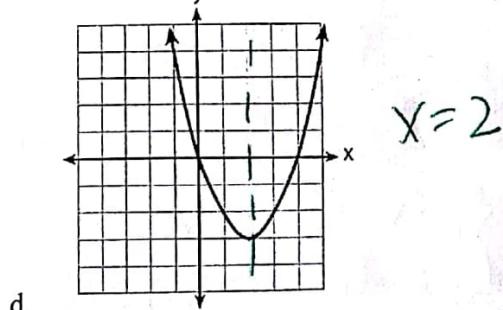
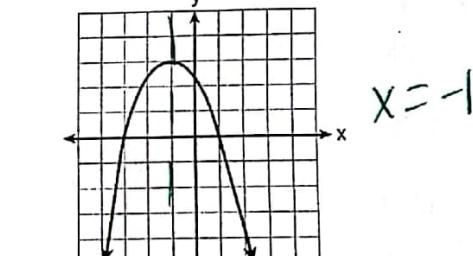
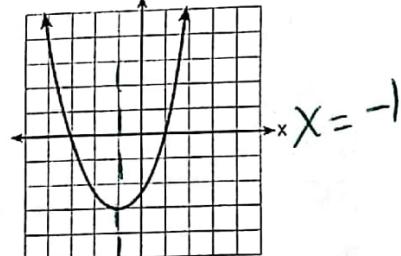
$$2 = 3(x + 1)^2$$

-2

$$\boxed{y = 3(x + 1)^2 - 2}$$

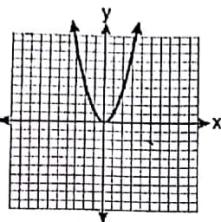
$$\boxed{\text{vertex: } (-1, -2)}$$

4. Which parabola has an axis of symmetry of  $x = 1$ ?

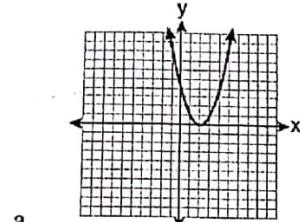


d.

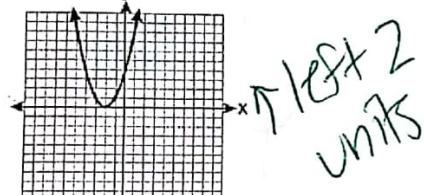
5. The graph below shows the function  $f(x)$ .



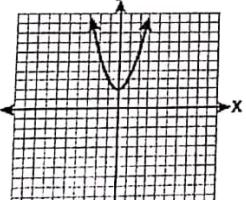
Which graph represents the function  $f(x+2)$ ?



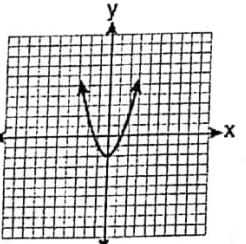
a.



(b)



c.



d.

$\uparrow 1 \text{ & } x^2 \text{ units}$

6. What is the result when  $4x^2 - 17x + 36$  is subtracted from  $2x^2 - 5x + 25$ ?

- a.  $6x^2 - 22x + 61$   
 b.  $2x^2 - 12x + 11$   
 c.  $-2x^2 - 22x + 61$   
 d.  $-2x^2 + 12x - 11$

7. When factored completely,  $x^3 - 13x^2 - 30x$  is

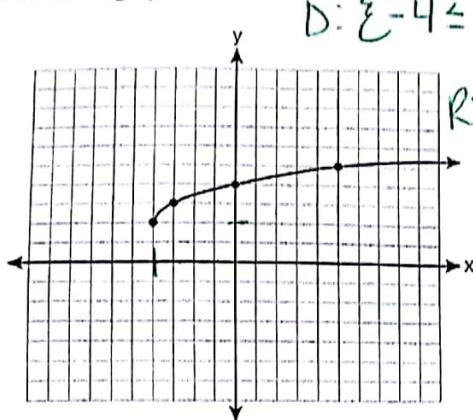
- a.  $x(x+3)(x-10)$   
 b.  $x(x-3)(x-10)$   
 c.  $x(x+2)(x-15)$   
 d.  $x(x-2)(x+15)$

GCF:  $x$   
 $x(x^2 - 13x - 30)$

$x(x-15)(x+2)$

**Short Answer-** Show ALL work to receive full credit.

8. What are the domain and the range of the function shown in the graph below?



9. 11. What is the vertex of the graph of the equation  $y = 3x^2 + 6x + 1$ ?

MUST show WORK!  

$$\begin{aligned} -1 &= 3(x^2 + 2x + 1) \\ -1 &= 3(x+1)^2 - 2 \end{aligned}$$

$$y = 3(x+1)^2 - 2$$

vertex:  $(-1, -2)$

10. a. Find a rule for a quadratic function that opens up and has x-intercepts of  $(-3, 0)$  and  $(5, 0)$ .

$y = a(x+3)(x-5)$ ,  
where  $a$  is any positive real #

- b. Without using your calculator, find the coordinates of the minimum point of the graph of your function in Part a.

$x = 1$  b/c 1 is between -3 and 5  
 $y$  is any value depending on the  $a$ -value you chose

Consider the quadratic function  $f(x) = x^2 - 12x + 27$ .

- a. Find the value of  $f(8)$ .

$$\begin{aligned} f(8) &= (8)^2 - 12(8) + 27 \\ &= 64 - 96 + 27 = \end{aligned}$$

- b. Find the y-intercept of the graph of  $f(x)$ .

$x$ -value is y-intercept so  
 $f(0) = 27$

12. Write a rule for a quadratic function with a graph that has x-intercepts  $(2, 0)$  and  $(-6, 0)$  and a maximum point of  $(-2, 4)$ .

$$y = a(x-2)(x+6)$$

$$4 = a(-2-2)(-2+6)$$

$$4 = a(-4)(4)$$

$$4 = a(-16)$$

$$a = -\frac{1}{4}$$

$$y = -\frac{1}{4}(x-2)(x+6)$$

Name: \_\_\_\_\_

ID: A

13. Write a rule for a quadratic function with a graph that has  $x$ -intercepts  $(-2, 0)$  and  $(8, 0)$  and  $y$ -intercept  $(0, 8)$ .

$$\begin{aligned}y &= a(x+2)(x-8) \\8 &= a(0+2)(0-8) \\8 &= a(2)(-8) \\8 &= a(-16) \\\frac{8}{-16} &= \frac{-1}{2} = a \\y &= -\frac{1}{2}(x+2)(x-8)\end{aligned}$$

14. a. Complete the square for the function  $2x^2 - 12x + 4 = 0$ .

$$\begin{aligned}2x^2 - 12x &= -4 \\2(x^2 - 6x + 9) &= -4 + 18 \\2(x-3)^2 &= 14 \\2(x-3)^2 - 14 &= y\end{aligned}$$

- b. What is the vertex of the quadratic function? Explain your reasoning.

$$(3, -14)$$

15. Rewrite each of these quadratic expressions in an equivalent factored form.

a.  $x^2 + 13x - 30$

$$(x-2)(x+15)$$

b.  $9x^2 - 25$

$$(3x-5)(3x+5)$$

c.  $28x^2 + 4x$

$$4x(7x+1)$$

d.  $x^2 - 18x + 81$

$$\begin{aligned}(x-9)(x-9) \\ \text{or} \\ (x-9)^2\end{aligned}$$

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16. Rewrite each sum or difference in standard polynomial form.

a.  $(5x^3 + 3x^2 - 4) + (x^4 - 3x^2 + 10)$

$$\boxed{x^4 + 5x^3 + 6}$$

b.  $(15 - 3x^3 + 4x) - (5x^3 + 8)$

$$\boxed{-8x^3 + 4x + 7}$$

17. Rewrite each of these quadratic expressions in equivalent standard form.

a.  $(x - 8)(x + 8)$

$$\boxed{x^2 - 64}$$

b.  $(2x + 7)(x + 3)$

$$\boxed{2x^2 + 13x + 21}$$

c.  $(x + 3)^2$

$$\boxed{x^2 + 6x + 9}$$

d.  $(x - 4)(x + 11)$

$$\boxed{x^2 + 7x - 44}$$

18.

Describe the transformations occurring from the parent function  $y = x^2$  to each of the following functions.

a.  $y = (x + 2)^2$

- left 2 units

b.  $y = -4x^2$

- reflect over the x-axis

- vertical stretch of 4

c.  $y = (x + 2)^2 - 3$

- left 2 units

d.  $y = \frac{2}{5}(x + 2)^2 + 1$

- vertical compression of  $2/5$ 

- left 2 units

- up 1 unit